

Problem 1. Estimate the area under the graph of $f(x) = 6x - x^2$ between $a = 0$ and $b = 6$ as follows:

- (a) Divide $[0, 6]$ into three equally sized intervals. Let Δx denote the length of one of these intervals.
- (b) Find the midpoint of each interval. Label these midpoints c_1 , c_2 , and c_3 .
- (c) Compute $\sum_{i=1}^3 f(c_i)\Delta x$.

Problem 2. Solve the initial value problem $y'(x) = 6x - x^2$ and $y(0) = 0$. Compute $y(6)$.

Problem 3 (Extra Credit). Compute the indefinite integral $\int 5x^4 \tan^2(x^5) dx$.